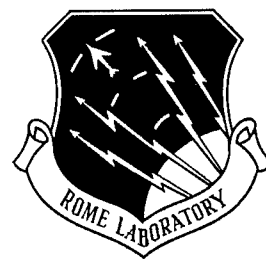


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MICROWAVE IMPEDANCE MATCHING OF PHOTODIODES FOR HIGH SPEED OPTICAL COMMUNICATIONS SYSTEMS

David A. Sumberg, Consultant

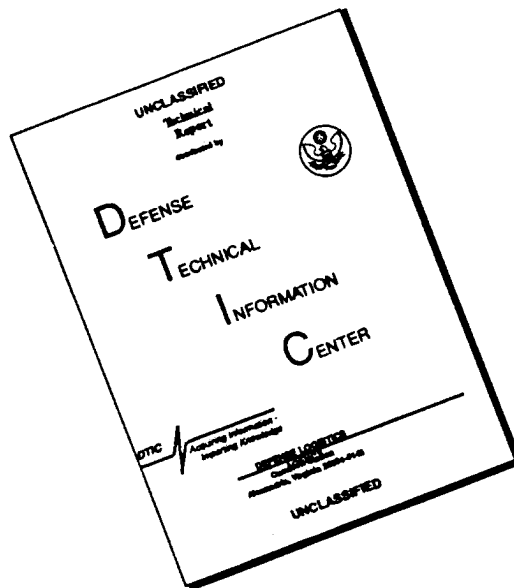
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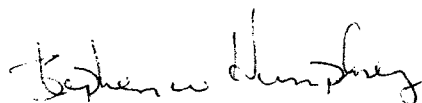
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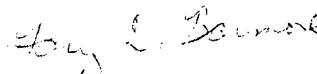
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TABLE OF CONTENTS

1	EXECUTIVE SUMMARY	1
2	MATHEMATICAL MODEL	2
2.1	INTRODUCTION AND BACKGROUND	2
2.2	MATHEMATICAL FORMULATION	3
3	EXPERIMENTAL DESIGN AND RESULTS	7
3.1	EQUALIZER DESIGN	7
3.2	EXPERIMENTAL RESULTS AND DISCUSSION	11
4	CONCLUSION	14
5	REFERENCES	15
	APPENDIX A	16
	APPENDIX B	20
	APPENDIX C	24
	APPENDIX D	26

LIST OF FIGURES

Figure 1. Block diagram of a system in which the equalizer matches the load to the generator.	2
Figure 2. Three element low-pass equalizer for laser diode (modeled as an LCR load).	3
Figure 3. Experimentally measured S_{11} parameter for a Sharp laser diode, type LTO22. Lower curve: $\text{Re}\{S_{11}\}$, middle curve: $\text{Im}\{S_{11}\}$, upper curve: $ S_{11} $.	5
Figure 4. Transducer power gain.	6
Figure 5. Transducer power gain.	6
Figure 6. Results of sensitivity analysis in which the values of L and C are varied by $\pm 10\%$ from their optimum values.	7
Figure 7. Transducer power gain.	10
Figure 8. Measured values of $T(\omega)$ for the five segment stepped-impedance equalizer terminated with the laser diode and the laser diode without the equalizer	11
Figure 9. Transducer power gain. Equalizer with stray capacitance.	12
Figure 10. Experimental apparatus used to measure S_{21} .	13
Figure 11. S_{21} for the load with equalizer and without equalizer	13

1 EXECUTIVE SUMMARY

Many factors influence the performance of an optical communication system. This report addresses one of those factors, viz., the impedance mismatch between a low impedance laser diode and the generator. Based on a technique first described by Carlin¹, a procedure is described for impedance matching the laser diode to a $50\ \Omega$ source over a prescribed frequency band by means of a lossless equalizer network. Carlin shows the form of the network to be that of a low-pass ladder circuit consisting of inductors and capacitors. The values for these unknown components are determined by maximizing, in a least-square sense, the transducer power gain over the prescribed frequency band. The procedure uses measured S_{11} data for the laser rather than deriving these values from an analytic model. The mathematical model predicts a 50% - 70% improvement in the transducer power gain and a flatter frequency response when compared with the laser diode alone.

In order to test the theory, a microstrip adaptation of the equalizer is designed based on stepped-impedance filter theory. The equalizer is fabricated and tested. Test results are found to be consistent with the results predicted by the model.

2 MATHEMATICAL MODEL

2.1 INTRODUCTION AND BACKGROUND

The problem of broad-band matching a load to a resistive generator, the so-called single matching problem, has been described by Carlin¹. The block diagram of Figure 1 illustrates the major components, i.e., the generator, the equalizer, and the load. The problem, of course, is to determine the exact form of the equalizer that will broad-band match the load to the generator.

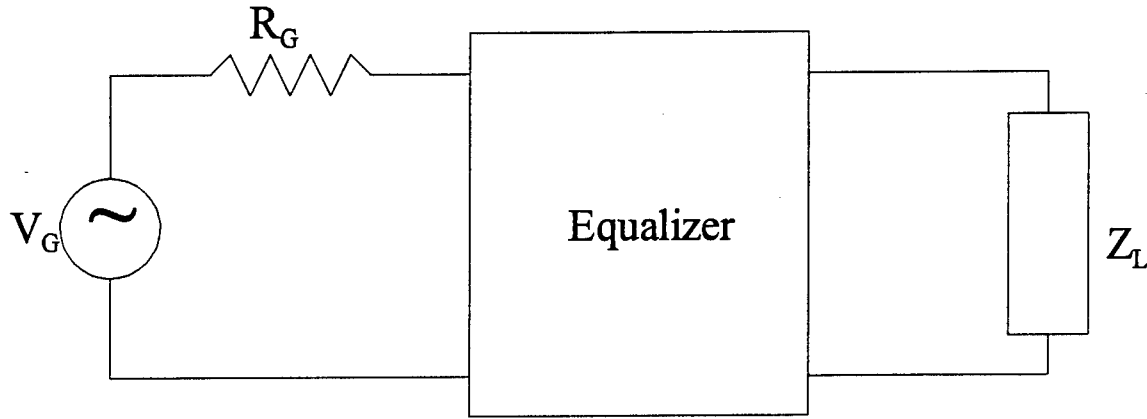


Figure 1. Block diagram of a circuit in which the equalizer matches the load to the generator.

Carlin approaches this problem by considering the transducer power gain $T(\omega^2)$ of the load-equalizer system, where

$$\begin{aligned} T(\omega^2) &= \frac{\text{Power to the load}}{\text{Power available from the generator}} = 1 - |\Gamma|^2 \\ &= \frac{4 R_L(\omega) R_q(\omega)}{|Z_L(\omega) + Z_q(\omega)|^2} \end{aligned} \quad (1)$$

In the above equations $\Gamma = (Z_L - Z_q)/(Z_L + Z_q)$ is the complex reflection coefficient at the load-equalizer interface, $Z_q(\omega) = R_q(\omega) + jX_q(\omega)$ is the equalizer impedance, and $Z_L(\omega) = R_L(\omega) + jX_L(\omega)$

is the known load impedance. Carlin solves the problem by representing $R_q(\omega)$, the real part of the equalizer impedance, as a number of straight line segments of unknown slopes between the frequency breakpoints $0 < \omega_1 < \omega_2 \dots < \omega_n$ spanning the passband, and choosing the slopes such that the transducer power gain is a maximum. The reactance $X_L(\omega)$ is then determined from $R_q(\omega)$ by a Hilbert transform. Once the line segments describing $R_q(\omega)$ are determined, this piecewise continuous function is approximated by a rational function of ω denoted by $\hat{R}_q(\omega)$. A rational function for $X_q(\omega)$ denoted by $\hat{X}_q(\omega)$ is determined as above by a Hilbert transform. Using the rational form of the impedance ($\hat{Z}_q(\omega) = \hat{R}_q(\omega) + j \hat{X}_q(\omega)$) the equalizer is realized as a Darlington reactance 2-port.

2.2 MATHEMATICAL FORMULATION

While Carlin's method provides a novel solution to the problem, it is not always the most straight-forward approach. In this report the problem of broad-band matching a laser diode to a 50 ohm generator is solved using a variation of the above technique. To begin, we note that a laser diode can be modeled as an LCR load, which Carlin shows is matched to the generator by a low-pass LC ladder network as in Figure 2. Thus, we postulate the form of the equalizer to be that of a low-

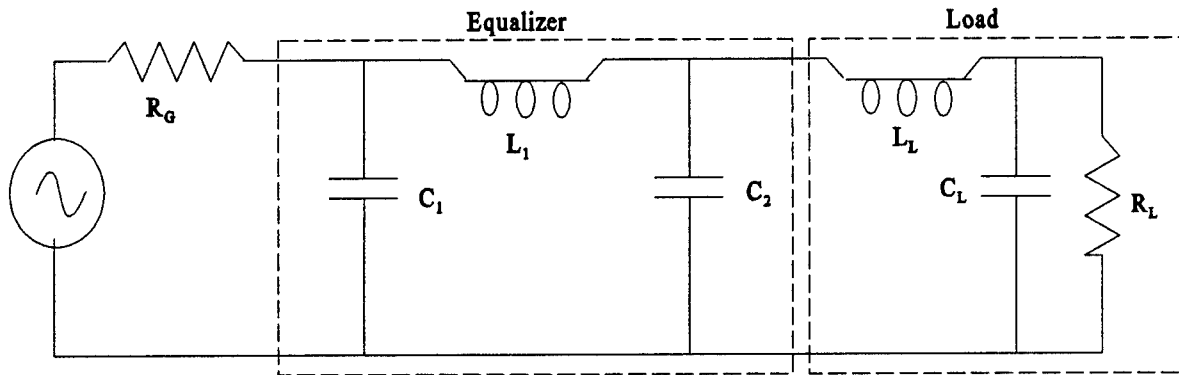


Figure 2. Three element low-pass equalizer for laser diode (modeled as an LCR load).

pass LC ladder network. We then write the transducer power gain in terms of the unknown parameters L and C and determine their values such that the transducer power gain is maximized.

Pozar² expresses the transducer power gain in terms of the scattering parameters S_{ij} of the equalizer as follows:

$$T(\omega^2) = \frac{|S_{21}(\omega)|^2 \cdot (1 - |S_G|^2) \cdot (1 - |S_L(\omega)|^2)}{|1 - S_{11}(\omega) \cdot S_G|^2 \cdot |1 - S_2(\omega) \cdot S_L(\omega)|^2} \quad (2)$$

where $S_L(\omega)$ is the experimentally determined reflection coefficient (S_{11}) at the load and is presented in Figure 3. The reflection coefficient at the generator is $S_G = (R_G - R_0)/(R_G + R_0)$, where R_0 is the characteristic line impedance and R_G is the generator resistance, and

$$S_2(\omega) = S_{22}(\omega) + \frac{S_{21}(\omega)^2 \cdot S_G}{1 - S_{22}(\omega) \cdot S_G} \quad (3)$$

For the case of a generator matched to the line ($R_G = R_0$), $S_G = 0$, and the following simplifications result:

$$S_2(\omega) = S_{22}(\omega) \quad (4)$$

and

$$T(\omega^2) = \frac{|S_{21}(\omega)|^2 \cdot (1 - |S_L(\omega)|^2)}{|1 - S_{22}(\omega) \cdot S_L(\omega)|^2} \quad (5)$$

The scattering parameters S_{ij} depend on the L and C components that comprise the equalizer. Expressions for the scattering parameters in terms of L and C are reproduced in Appendix A for a three element low-pass ladder network and in Appendix B for a five element low-pass ladder network.

Optimization is carried out for the load of Figure 3. The data, which represents $|S_L(\omega)|^2$ in Eq (5), is obtained using a network analyzer to measure S_{11} with the laser biased at its operating point. The transducer power gain is then optimized in a least-square sense by minimizing the following function:

$$SSE = \sum_{i=1}^n [T(\omega_i) - T_I]^2 \quad (6)$$

where T_I is the idealized value for $T(\omega)$ and must be in the range (0, 1). SSE is the sum of the square of the errors. Several currently available software packages, Mathcad and Matlab to name but two, have built-in optimization capability. The specific results presented in this report were obtained using Mathcad's "minerr" function.

The resulting values for C and L for the three and five element networks are summarized in Table 1. The transducer power gains with and without the equalizer network are plotted in Figure 4 for the three element network and in Figure 5 for the five element network. Detailed information for the three and five element networks appear in Appendix A and Appendix B, respectively.

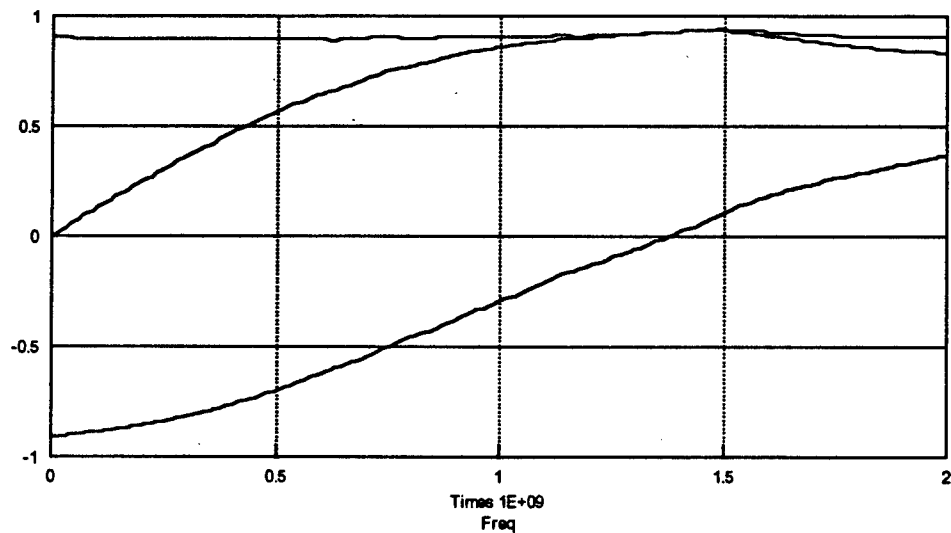


Figure 3. Experimentally measured S_{11} parameter for a Sharp laser diode, type LTO22. Lower curve: $\text{Re}\{S_{11}\}$, middle curve: $\text{Im}\{S_{11}\}$, upper curve: $|S_{11}|$.

Table 1. Component values		
	3 elements	5 elements
C_1 (pF)	1.90	1.44
C_2 (pF)	3.80	1.30
C_3 (pF)	N.A.	3.84
L_1 (nH)	6.51	2.20
L_2 (nH)	N.A.	5.41

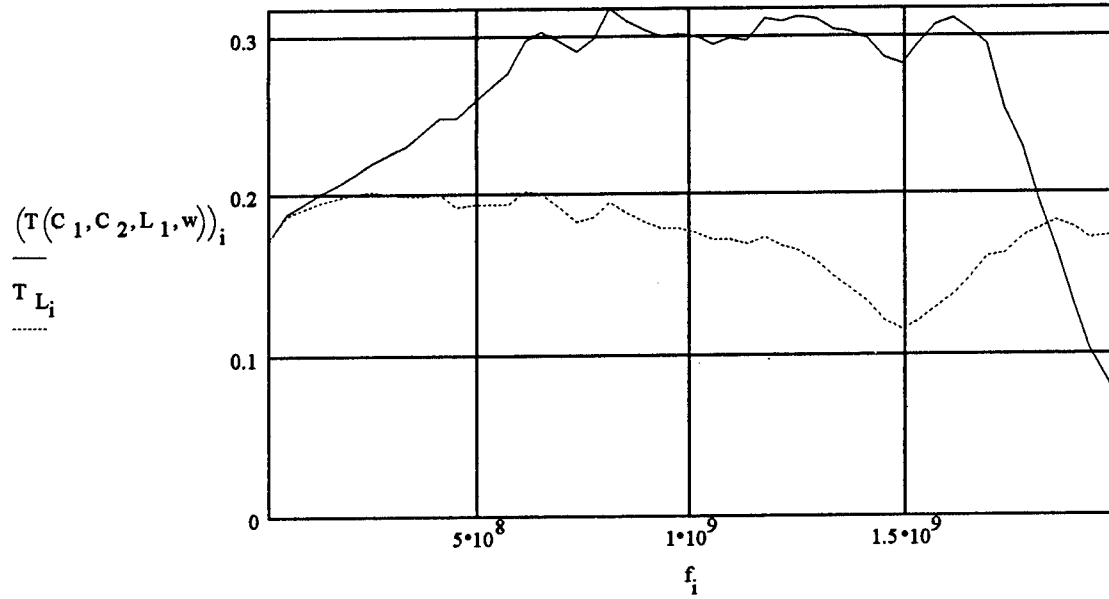


Figure 4. Transducer power gain. **Solid curve:** Three-element equalizer terminated with laser diode. Values for C_1 , C_2 , and L_1 are listed in Table 1. **Dashed curve:** Transducer power gain for the laser diode without equalizer.

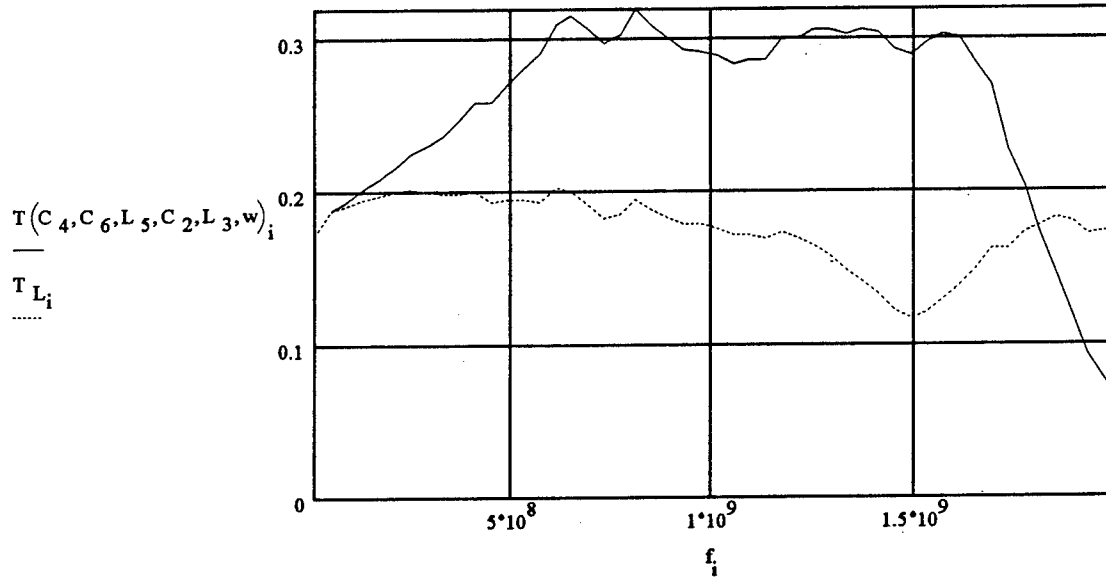


Figure 5. Transducer power gain. **Solid curve:** Five-element equalizer terminated with laser diode. Values for C_1 , C_2 , C_3 , L_1 , and L_2 are listed in Table 1. **Dashed curve:** Transducer power gain for the laser diode without equalizer.

3 EXPERIMENTAL DESIGN AND RESULTS

3.1 EQUALIZER DESIGN

The transition from the mathematical model to an actual physical realization of the equalizer is hampered by the difficulty in obtaining discrete components (capacitors and inductors) of the exact values required. The problem is further exacerbated by the sensitivity of the equalizer circuit to the values of the components. The results of a sensitivity analysis in which the values of L and C are varied by $\pm 10\%$ in the mathematical model is shown in Figure 6. It should be noted that small variations in the values of the components tend to destroy much of the potential benefits of the equalizer.

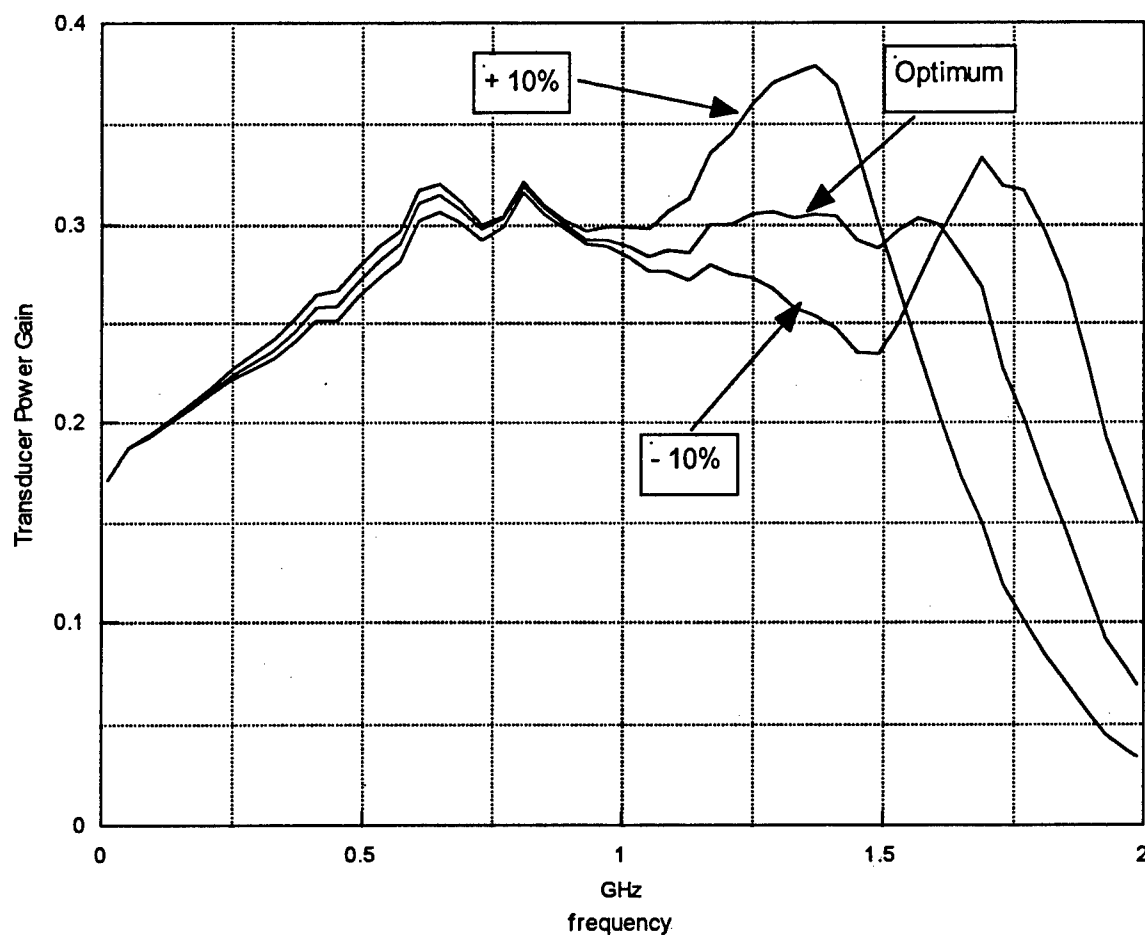


Figure 6. Results of sensitivity analysis in which the values of L and C are varied by $\pm 10\%$ from their optimum values.

Based on these observations, a practical solution is to employ microstrip design techniques to fabricate the required equalizer network. Of the several choices available, a stepped-impedance filter design is selected, because of its ease of fabrication. As is well known, the stepped impedance design substitutes a series combination of high and low impedance transmission lines for the components of the ladder network; high impedance lines replace inductors while low impedance lines replace capacitors. A summary of the microstrip design equations used in this report may be found in Appendix C. An example of a stepped impedance design fabricated on microstrip is shown in Appendix D.

The parameters to be determined for the stepped impedance filter are the length and width of each line segment. As a practical matter, line widths are limited to values between (approximately) 0.1 mm and 35 mm. According to the theory of microstrip lines summarized in Appendix C, the stated range of line widths confine the characteristic impedance of the transmission line to values between (approximately) 20 Ω and 200 Ω . See the figure of Appendix C for a plot of characteristic impedance vs. line width for typical Duroid material.

When designing a stepped-impedance filter, standard approximations⁴ are used to calculate the length of each line segment based on the value of the inductor or capacitor that it replaces and by the characteristic impedance of the transmission line. However, rather than simply use the approximations to translate the previously determined values of L and C to transmission line lengths, the lengths of the transmission lines are themselves treated as variables to be determined by the optimization process. This is achieved by first writing the scattering parameters in terms of the lengths of the line segments by means of the ABCD matrices (see below), and then by writing the transducer power gain in terms of the scattering parameters and optimizing the response, as was done previously. This calculation is more precise, since it uses the exact transmission line equations rather than the approximations referred to above. The relevant equations are stated below.

The ABCD matrix for the i^{th} transmission line segment⁵ of length ℓ_i is

$$M_i = \begin{bmatrix} \cos(\beta_i \ell_i) & jZ_i \sin(\beta_i \ell_i) \\ jY_i \sin(\beta_i \ell_i) & \cos(\beta_i \ell_i) \end{bmatrix} \quad (7)$$

where Z_i is the characteristic impedance of the line segment, $Y_i = 1/Z_i$, $\beta_i = 2\pi f/u_i$, with the phase velocity defined as $u_i = c/(\epsilon_e)^{1/2}$. The effective dielectric constant ϵ_e is defined in Appendix C. The overall ABCD matrix for n line segments is then the product of the individual matrices written as

$$M = M_1 \cdot M_2 \cdots M_n = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \quad (8)$$

where M_1 is the segment nearest the generator. Finally, the scattering parameters are obtained according to the following transformations⁵:

$$\begin{aligned} S_{11} &= \frac{A + \frac{B}{Z_0} - C \cdot Z_0 - D}{K} \\ S_{22} &= \frac{-A + \frac{B}{Z_0} - C \cdot Z_0 + D}{K} \\ S_{12} &= S_{21} = \frac{2}{K} \end{aligned} \quad (9)$$

where

$$K = A + \frac{B}{Z_0} + C \cdot Z_0 + D$$

Appendix D contains detailed calculations in which the above procedure is applied to a five element equalizer network. Table 2 summarizes the results of those calculations and includes the length, width, and characteristic impedance of each line segment as it appears in the final design. Lengths $\ell_1 - \ell_5$ represent the five elements, while length ℓ_0 of the 50 Ω line joining the generator and the equalizer is arbitrary. The transducer power gain with and without the equalizer is plotted in Figure 7.

Table 2. Segment Lengths			
	length in mm.	width in mm.	characteristic impedance (Ω)
ℓ_0	-	9.43	50
ℓ_1	6.75	31.6	200
ℓ_2	2.72	0.308	20
ℓ_3	6.19	31.6	200
ℓ_4	5.23	0.308	20
ℓ_5	15.83	31.6	200

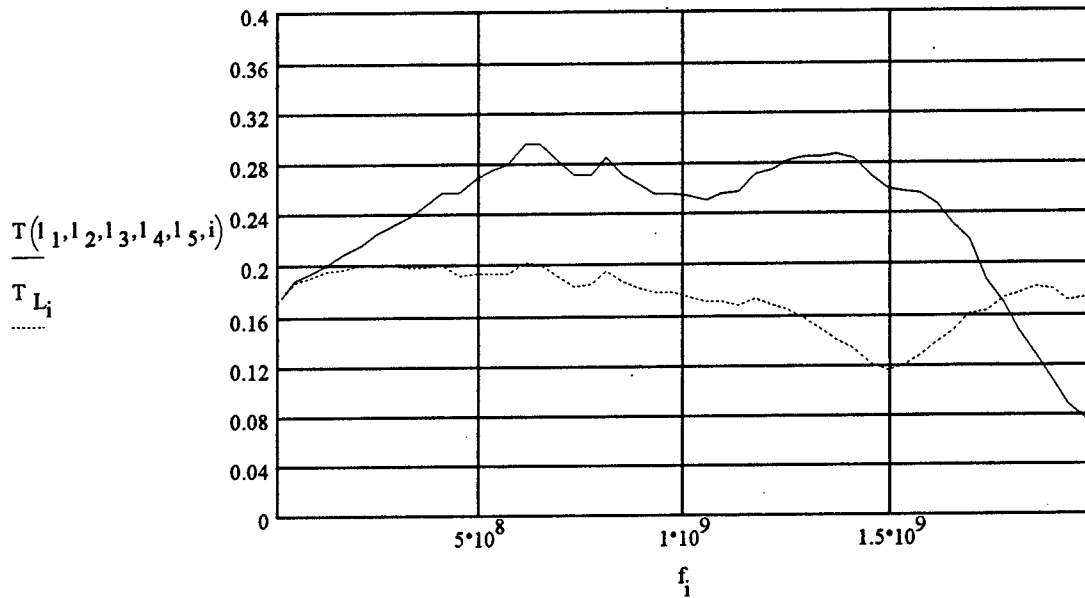


Figure 7. Transducer power gain. **Solid curve:** Five-segment stepped-impedance equalizer terminated with laser diode. Values for $\ell_1 - \ell_5$ are listed in Table 2. **Dashed curve:** Transducer power gain for the laser diode without equalize

3.2 EXPERIMENTAL RESULTS AND DISCUSSION

The experimental results consist of two sets of data: (1) the transducer power gain and (2) S_{21} . Measured values of transducer power gain are presented in Figure 8 and Figure 9. The data of Figure 8 represents $T(\omega)$ for the load with and without the equalizer. The data of Figure 9 is $T(\omega)$ when a small amount of stray capacitance is introduced by placing a finger near one of the line segments. Figure 9 is included, because it suggests the possibility that different architectures (perhaps a capacitor in parallel with one of the inductors) may result in greater values of $T(\omega)$. It also illustrates

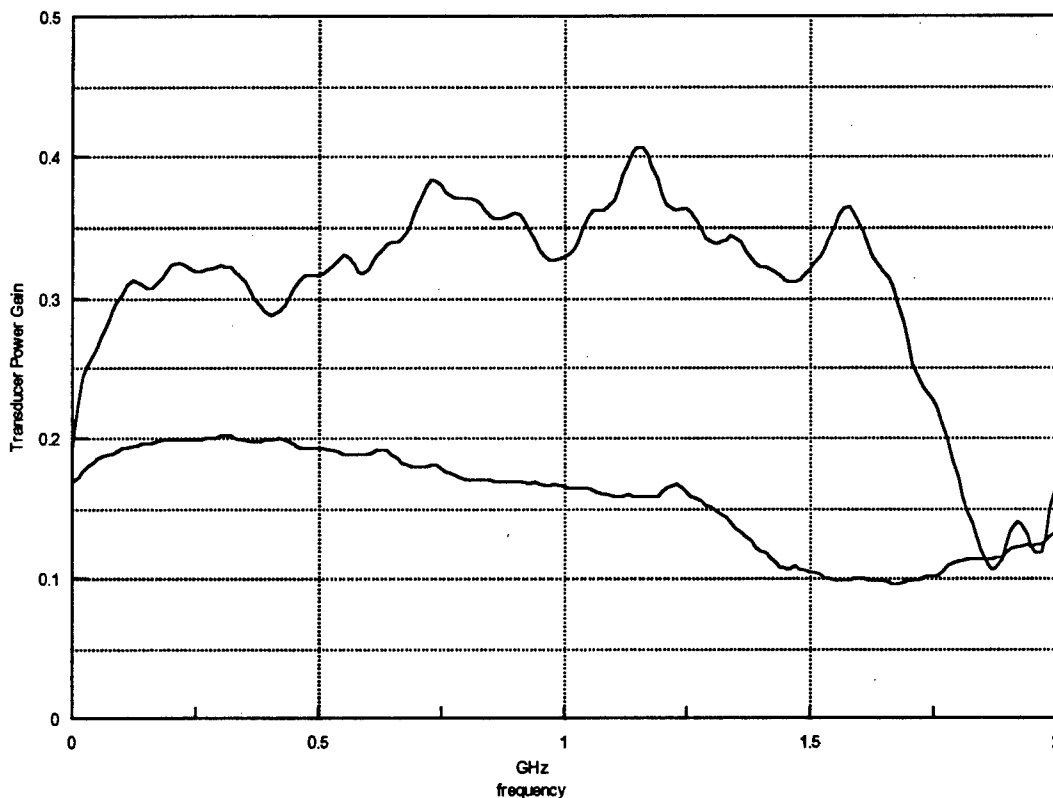


Figure 8. Measured values of $T(\omega)$ for the five segment stepped-impedance equalizer terminated with the laser diode (upper curve) and the laser diode without the equalizer (lower curve).

how the optimization process may be dependent on the guessed values that are used to initiate the process, i.e., different initial values may produce a different outcome. Comparison of Figure 8 with Figure 7 shows a somewhat better gain than anticipated, perhaps caused by the influence of stray capacitance.

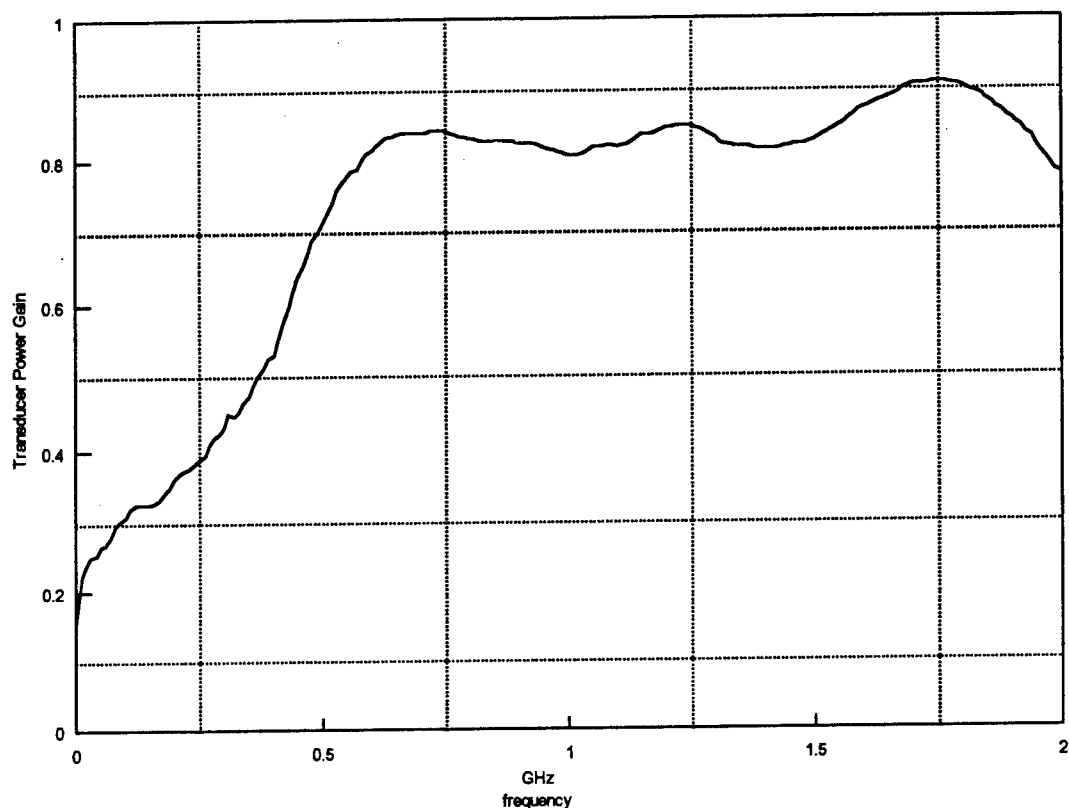


Figure 9. Transducer power gain. Equalizer with stray capacitance.

The second set of data is a measurement of S_{21} . The apparatus used to obtain these data is shown in Figure 10. The data itself is plotted in Figure 11, which shows S_{21} for the laser diode with and without the equalizer. A comparison of the two curves of Figure 11 shows a significant improvement in frequency response over the range 0 - 1.25 GHz. The equalizer provides a frequency response that is flat to within 3 dB, whereas without the equalizer the response fluctuates by more than 10 dB.

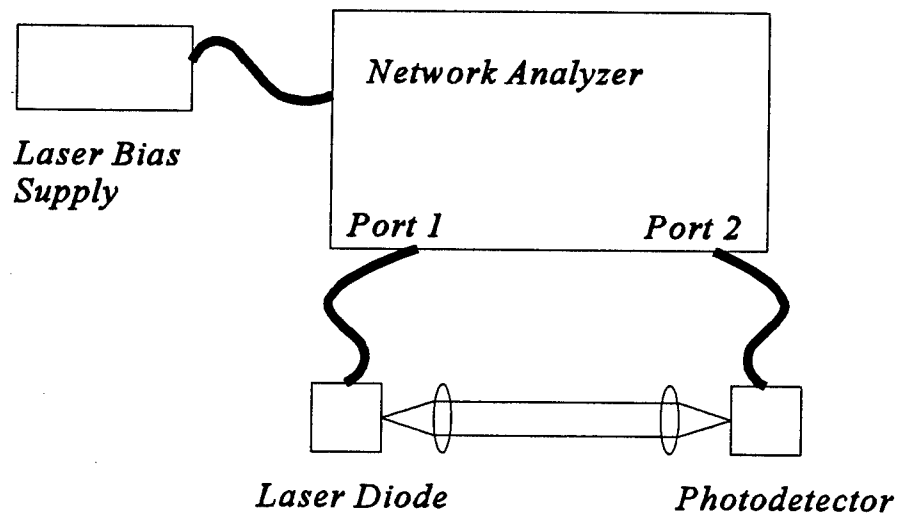


Figure 10. Experimental apparatus used to measure S_{21} .

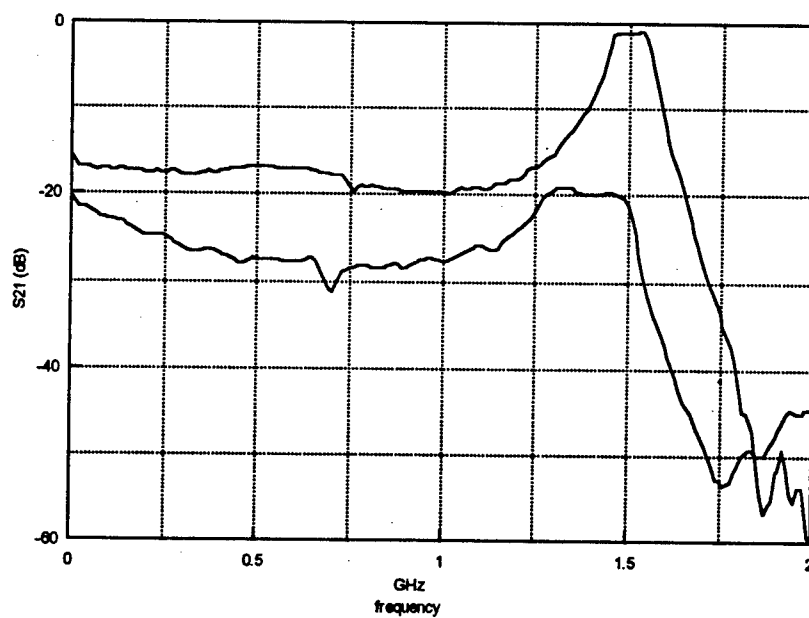


Figure 11. S_{21} for the load with equalizer (upper curve) and without equalizer (lower curve).

4 CONCLUSION

This report describes a procedure for impedance matching a low impedance laser diode to a $50\ \Omega$ source over a prescribed frequency band by means of a lossless equalizer network. The form of the network is that of a low-pass ladder circuit consisting of inductors and capacitors. The values for these unknown components are determined from measured S_{11} data for the laser diode by maximizing, in a least-square sense, the transducer power gain over the prescribed frequency band. Based on the derived component values, the theory predicts a 50% - 70% improvement in the transducer power gain and a flatter frequency response when compared with the laser diode alone.

A microstrip adaptation of the equalizer is designed based on stepped-impedance filter theory. The equalizer is fabricated and tested. Test results confirm the 50% - 70% performance improvement predicted by the model. S_{21} measurements show a 3 dB fluctuation in the frequency response compared with 10 dB for the laser diode without the equalizer.

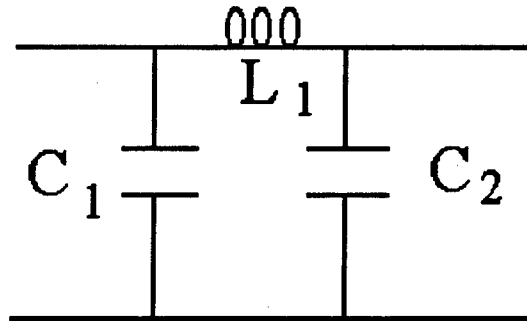
Finally, during system testing it was shown that stray capacitance resulted in transducer power gains of nearly 80%. This observation suggests that future activity should center on alternative architectures for the equalizer, particularly those which place capacitors in parallel with the inductors.

5 REFERENCES

1. H. J. Carlin, "A new approach to gain-bandwidth problems," *IEEE Trans. Circuits Syst.*, vol. CAS-24, pp. 170-175, Apr. 1977
2. Ibid.
3. D. M. Pozar, *Microwave Engineering*, Reading, MA, Addison-Wesley, 1990, p 243
4. Ibid. See, for example, equations 9.86a and 9.86b on p. 503.
5. Ibid. See Table 5.1, p233.
6. Ibid. See Table 5.2, p235.

APPENDIX A

Optimization for a 3-element low-pass equalizer (pi-section consisting of C_1 , C_2 , L_1).
The following calculation was written using Mathcad 5.0.



Characteristic line impedance; Impedance of the generator

$$R_0 := 50$$

$$R_g := 50$$

Read from disk the data file for the laser diode.

$A := \text{READPRN}(\text{comb_sht})$

$f := A^{<1>}$

$w := 2 \cdot \pi \cdot f$

$n := \text{length}(w)$

$n = 11$

$i := 1..n$

Define reactance of the elements

$$x_{C1}(C_1) := \frac{1}{j \cdot C_1 \cdot w}$$

$$x_{C2}(C_2) := \frac{1}{j \cdot C_2 \cdot w}$$

$$x_{L1}(L_1) := j \cdot w \cdot L_1$$

Input Admittance and Impedance looking into port 1 when the output is terminated with R_0

$$Y_{in1}(C_1, C_2, L_1) := \frac{\frac{1}{x_{C1}(C_1)} + \frac{1}{x_{L1}(L_1) + \frac{1}{\frac{1}{x_{C2}(C_2)} + \frac{1}{R_0}}}}{1}$$

$$Z_{in1}(C_1, C_2, L_1) := \frac{1}{Y_{in1}(C_1, C_2, L_1)}$$

Input Admittance and Impedance looking into port 2 when the input is terminated with R_0

$$Y_{in2}(C_1, C_2, L_1) := \frac{\frac{1}{x_{C2}(C_2)} + \frac{1}{x_{L1}(L_1) + \frac{1}{\frac{1}{x_{C1}(C_1)} + \frac{1}{R_0}}}}{1}$$

$$Z_{in2}(C_1, C_2, L_1) := \frac{1}{Y_{in2}(C_1, C_2, L_1)}$$

Scattering matrix elements for the equalizer

$$S_{11}(C_1, C_2, L_1) := \frac{Z_{in1}(C_1, C_2, L_1) - R_0}{Z_{in1}(C_1, C_2, L_1) + R_0}$$

$$S_{22}(C_1, C_2, L_1) := \frac{Z_{in2}(C_1, C_2, L_1) - R_0}{Z_{in2}(C_1, C_2, L_1) + R_0}$$

$$S_{12}(C_1, C_2, L_1) := \frac{1 + S_{22}(C_1, C_2, L_1)}{1 + x_{L1}(L_1) \cdot \left(\frac{1}{R_0} + \frac{1}{x_{C1}(C_1)} \right)}$$

$$S_{21}(C_1, C_2, L_1) := \frac{1 + S_{11}(C_1, C_2, L_1)}{1 + x_{L1}(L_1) \cdot \left(\frac{1}{R_0} + \frac{1}{x_{C2}(C_2)} \right)}$$

Read (from disk) the scattering matrix (reflection coef) for the laser diode at frequencies f_i

$$S_L := A^{\langle 2 \rangle} + j \cdot A^{\langle 3 \rangle}$$

$$m := \text{length}(S_L)$$

$$m = 11$$

Scattering matrix (reflection coef) for the generator at frequencies f_i

$$S_g := \frac{R_g - R_0}{R_g + R_0} \quad S_g = 0$$

Transducer power gain

$$S_2(C_1, C_2, L_1) := \overrightarrow{\left(S_{22}(C_1, C_2, L_1) + \frac{S_{21}(C_1, C_2, L_1)^2 \cdot S_g}{1 - S_{22}(C_1, C_2, L_1) \cdot S_g} \right)}$$

$$T(C_1, C_2, L_1, w) := \frac{\left(|S_{21}(C_1, C_2, L_1)| \right)^2 \cdot \left[1 - \left(|S_g| \right)^2 \right] \cdot \left[1 - \left(|S_L| \right)^2 \right]}{\left(|1 - S_{11}(C_1, C_2, L_1) \cdot S_g| \right)^2 \cdot \left(|1 - S_2(C_1, C_2, L_1) \cdot S_L| \right)^2}$$

Calculate the component values (C_1 , etc.) that maximize the transducer power gain T at the frequencies f_i (in a least-squares sense).

Set the idealized value for T (this is arbitrary)

$$T_I := 0.30$$

Compute the sum of the squares, which is to be minimized

$$\text{SSE}(C_1, C_2, L_1) := \sum_{i=1}^n \left(T(C_1, C_2, L_1, w)_i - T_I \right)^2$$

Initial guess for parameters

$$C_1 := 1.904314 \cdot 10^{-12}$$

$$C_2 := 3.8038 \cdot 10^{-12}$$

$$L_1 := 6.50727 \cdot 10^{-9}$$

Set up a solve block

Given

$$\text{SSE}(C_1, C_2, L_1) = 0$$

Dummy equations: Mathcad needs 3 equations for 3 unknowns

$$1 = 1$$

$$2 = 2$$

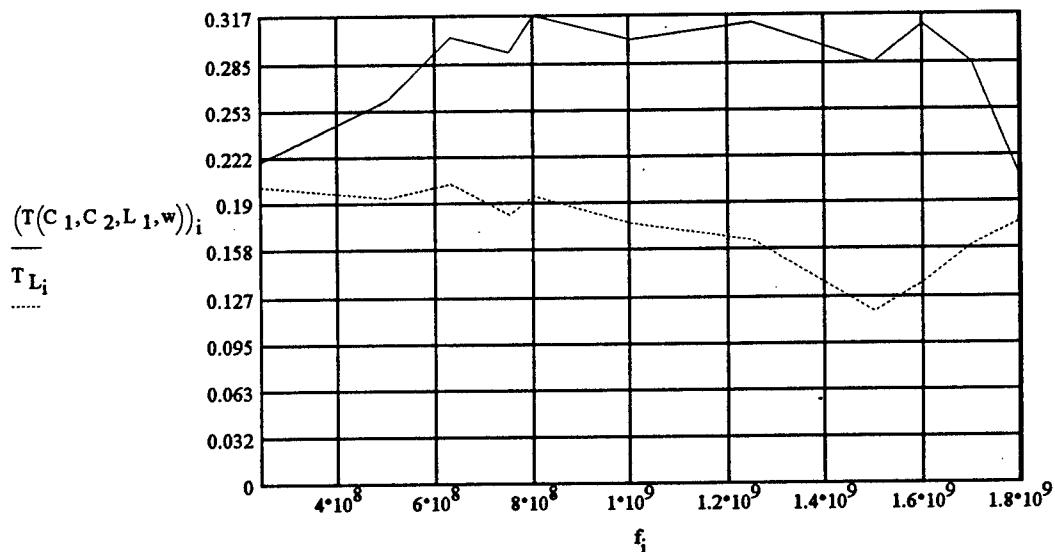
Minerr function gives best fit to data

$$\begin{bmatrix} C_1 \\ C_2 \\ L_1 \end{bmatrix} := \text{Minerr}(C_1, C_2, L_1) \quad \begin{bmatrix} C_1 \\ C_2 \\ L_1 \end{bmatrix} = \begin{bmatrix} 1.90431 \cdot 10^{-12} \\ 3.8038 \cdot 10^{-12} \\ 6.50727 \cdot 10^{-9} \end{bmatrix}$$

Calculate the transducer power gain for the laser diode without the equalizer (assume $S_g = 0$) and calculate the mean-square error.

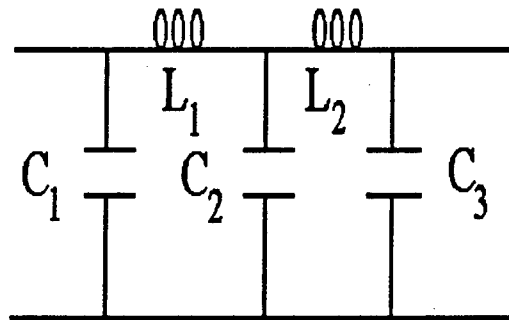
$$T_L := \overline{1 - (|S_L|)^2} \quad \frac{\text{SSE}(C_1, C_2, L_1)}{n - 2} = 0.002$$

Plot the transducer power gain with and without the equalizer



APPENDIX B

Optimization for a 5-element low-pass equalizer (pi-section consisting of C_1 , C_2 , C_3 , L_1 , L_2).
The following calculation was written using Mathcad 5.0



Characteristic line impedance; Impedance of the generator

$$R_0 := 50$$

$$R_g := 50$$

Read from disk the data file for the laser diode. Specify the frequency f_i as the 1st column.

$A := \text{READPRN}(\text{comb_sht})$

$f := A^{<1>}$

$w := 2 \cdot \pi \cdot f$

$n := \text{length}(w)$

$n = 11$

$i := 1..n$

Input Impedance looking into port 1 when the output is terminated with R_0

$$Z_{\text{inl}}(C_1, C_2, C_3, L_1, L_2) := \frac{1}{j \cdot w \cdot C_1 + \frac{1}{j \cdot w \cdot L_1 + \frac{1}{j \cdot w \cdot C_2 + \frac{1}{j \cdot w \cdot L_2 + \frac{1}{j \cdot w \cdot C_3 + \frac{1}{R_0}}}}}}$$

Input Impedance looking into port 2 when the input is terminated with R_0

$$Z_{in2}(C_1, C_2, C_3, L_1, L_2) := \frac{1}{j \cdot \omega \cdot C_3 + \frac{1}{j \cdot \omega \cdot L_2 + \frac{1}{j \cdot \omega \cdot C_2 + \frac{1}{j \cdot \omega \cdot L_1 + \frac{1}{j \cdot \omega \cdot C_1 + \frac{1}{R_0}}}}}}$$

Scattering matrix elements for the equalizer

$$S_{11}(C_1, C_2, C_3, L_1, L_2) := \frac{Z_{in1}(C_1, C_2, C_3, L_1, L_2) - R_0}{Z_{in1}(C_1, C_2, C_3, L_1, L_2) + R_0}$$

$$S_{22}(C_1, C_2, C_3, L_1, L_2) := \frac{Z_{in2}(C_1, C_2, C_3, L_1, L_2) - R_0}{Z_{in2}(C_1, C_2, C_3, L_1, L_2) + R_0}$$

$$S_{21}(C_1, C_2, C_3, L_1, L_2) := \frac{1 + S_{11}(C_1, C_2, C_3, L_1, L_2)}{1 + j \cdot \omega \cdot L_2 \cdot \left(\frac{1}{R_0} + j \cdot \omega \cdot C_3 \right)} \cdot \frac{1}{1 + j \cdot \omega \cdot L_1 \cdot \left[j \cdot \omega \cdot C_2 + \frac{1}{j \cdot \omega \cdot L_2 + \frac{1}{j \cdot \omega \cdot C_3 + \frac{1}{R_0}}} \right]}$$

$$S_{12}(C_1, C_2, C_3, L_1, L_2) := S_{21}(C_1, C_2, C_3, L_1, L_2)$$

Read (from disk) scattering matrix (reflection coef) for the laser diode at frequencies f_i

$$S_L := A^{<2>} + j \cdot A^{<3>}$$

$$m := \text{length}(S_L)$$

$$m = 11$$

Scattering matrix (reflection coef) for the generator at frequencies f_i

$$S_g := \frac{R_g - R_0}{R_g + R_0} \quad S_g = 0$$

Transducer power gain

$$S_2(C_1, C_2, C_3, L_1, L_2) := \overrightarrow{\left(S_{22}(C_1, C_2, C_3, L_1, L_2) + \frac{S_{21}(C_1, C_2, C_3, L_1, L_2)^2 \cdot S_g}{1 - S_{22}(C_1, C_2, C_3, L_1, L_2) \cdot S_g} \right)}$$

$$T(C_1, C_2, C_3, L_1, L_2, w) := \frac{\left(|S_{21}(C_1, C_2, C_3, L_1, L_2)| \right)^2 \cdot \left[1 - \left(|S_g| \right)^2 \right] \cdot \left[1 - \left(|S_L| \right)^2 \right]}{\left(|1 - S_{11}(C_1, C_2, C_3, L_1, L_2) \cdot S_g| \right)^2 \cdot \left(|1 - S_2(C_1, C_2, C_3, L_1, L_2) \cdot S_L| \right)^2}$$

Calculate the component values (C_1 , etc.) that maximize the transducer power gain T at the frequencies f_i (in a least-squares sense).

Set the idealized value for T (this is arbitrary)

$$T_I := 0.29$$

Compute the sum of the squares, which is to be minimized

$$SSE(C_1, C_2, C_3, L_1, L_2) := \sum_{i=1}^n \left(T(C_1, C_2, C_3, L_1, L_2, w)_i - T_I \right)^2$$

Initial guess for parameters

$$C_1 := 1.435 \cdot 10^{-12} \quad C_2 := 1.3 \cdot 10^{-12} \quad C_3 := 3.835 \cdot 10^{-12} \quad L_1 := 2.2 \cdot 10^{-9} \quad L_2 := 5.4065 \cdot 10^{-9}$$

Set up a solve block

Given

$$SSE(C_1, C_2, C_3, L_1, L_2) = 0$$

Dummy equations: Mathcad needs 5 equations for 5 unknowns

1=1 2=2 3=3 4=4

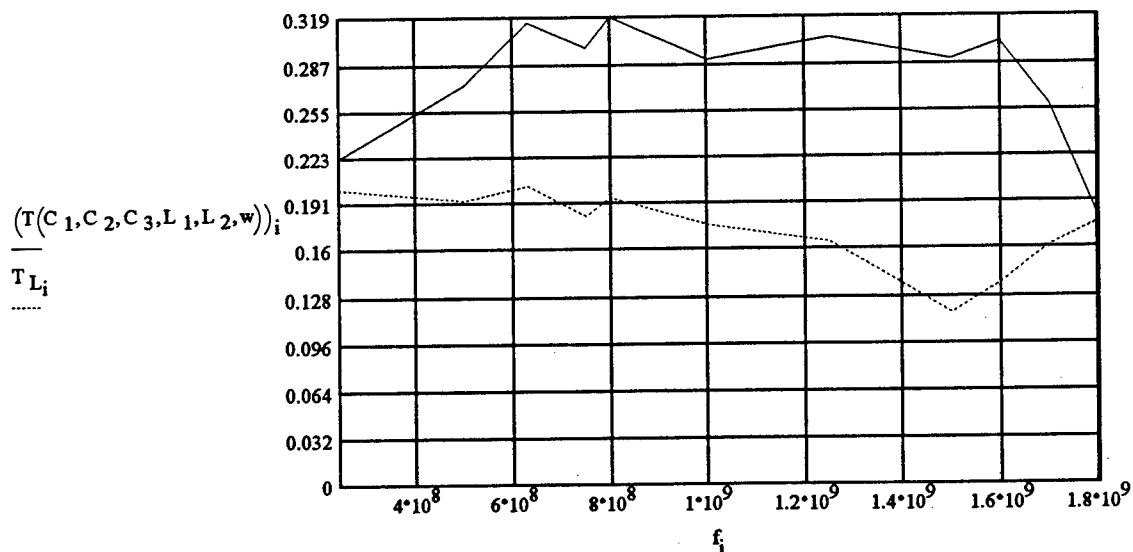
Minerr function gives best fit to data

$$\begin{bmatrix} C_1 \\ C_2 \\ C_3 \\ L_1 \\ L_2 \end{bmatrix} := \text{Minerr}(C_1, C_2, C_3, L_1, L_2) \quad \begin{bmatrix} C_1 \\ C_2 \\ C_3 \\ L_1 \\ L_2 \end{bmatrix} = \begin{bmatrix} 1.435 \cdot 10^{-12} \\ 1.3 \cdot 10^{-12} \\ 3.835 \cdot 10^{-12} \\ 2.2 \cdot 10^{-9} \\ 5.407 \cdot 10^{-9} \end{bmatrix}$$

Calculate the transducer power gain for the laser diode without the equalizer (assume $S_g = 0$)
the mean square error

$$T_L := \overline{1 - (|S_L|)^2} \quad \frac{\text{SSE}(C_1, C_2, C_3, L_1, L_2)}{n - 2} = 0.002$$

Plot the transducer power gain with and without the equalizer.



APPENDIX C

A SUMMARY OF MICROSTRIP EQUATIONS

1. Impedance of a microstrip line given the "width" to "dielectric thickness" ratio ($r=W/d$).

W = width; d = thickness of dielectric ; $r = W/d$

Define $a(r)$ such that:

$$a(r) = 1 \quad \text{if } 0 \leq r \leq 1$$

$$a(r) = 0 \quad \text{otherwise}$$

$$a(r) := \text{if}(r \leq 1, 1, 0)$$

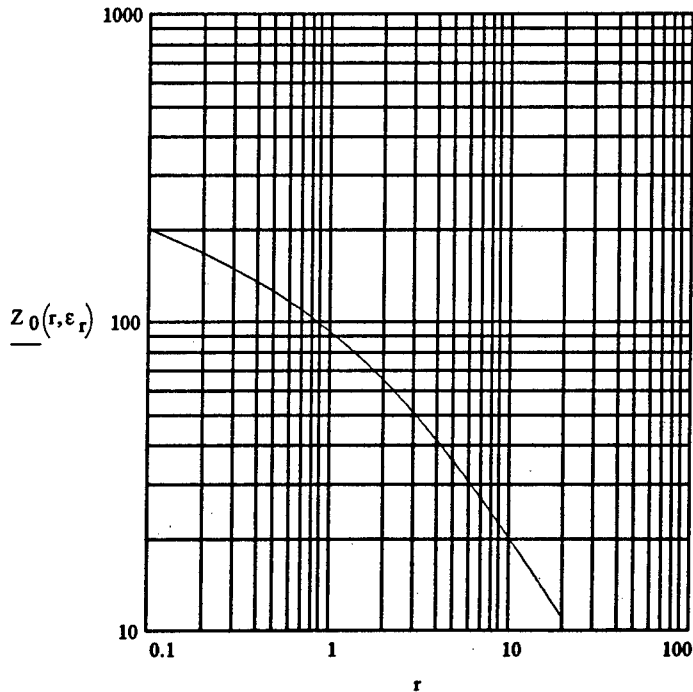
Effective dielectric constant:

$$\epsilon_e(r, \epsilon_r) := \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \cdot \left[\frac{1}{\sqrt{1 + \frac{12}{r}}} + a(r) \cdot 0.041 \cdot (1 - r)^2 \right]$$

Impedance [formulas from Pozar³ (p. 183)]

$$Z_0(r, \epsilon_r) := \frac{60}{\sqrt{\epsilon_e(r, \epsilon_r)}} \cdot \left[a(r) \cdot \ln\left(\frac{8}{r} + \frac{r}{4}\right) + (1 - a(r)) \cdot \frac{2 \cdot \pi}{(r + 1.393 + 0.667 \cdot \ln(r + 1.444))} \right]$$

Dielectric constant : $\epsilon_r := 2.33$



2. Width (W) of the Microstrip line

Calculate "r" (=W/d) given ϵ_r and Z_0 (Pozar p. 185) .

$$A(Z_0) := \frac{Z_0}{60} \cdot \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \cdot \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B(Z_0) := \frac{377 \cdot \pi}{2 \cdot Z_0 \cdot \sqrt{\epsilon_r}}$$

Pozar gives the following two equations for r depending on whether $r > 2$ or $r < 2$.

$$r_1(Z_0) := \frac{8 \cdot e^{A(Z_0)}}{e^{2 \cdot A(Z_0)} - 2} \quad \text{for } r < 2.$$

$$r_2(Z_0) := \frac{2}{\pi} \cdot \left[B(Z_0) - 1 - \ln(2 \cdot B(Z_0) - 1) + \frac{\epsilon_r - 1}{2 \cdot \epsilon_r} \cdot \left(\ln(B(Z_0) - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right) \right] \quad \text{for } r > 2.$$

The following equation for $r = W/d$ selects either r_1 or r_2 , depending on whether $r_1 < 2$ or $r_1 > 2$

$$r(Z_0) := \text{if}(r_1(Z_0) \leq 2, r_1(Z_0), r_2(Z_0))$$

Linewidths for extreme values of Z_0

$$Z_0 := 200$$

$$r(Z_0) = 0.09709$$

$$\text{Let } d := 0.125 \text{ inch}$$

$$d := d \cdot 25.4 \text{ mm}$$

$$W := r(Z_0) \cdot d \quad W = 0.30825 \text{ mm}$$

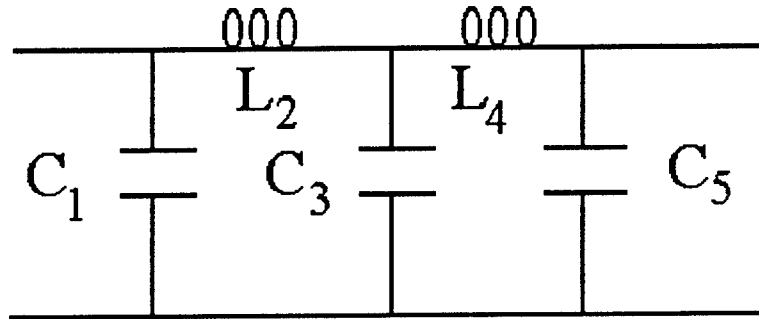
$$Z_0 := 20$$

$$r(Z_0) = 9.95253$$

$$W := r(Z_0) \cdot d \quad W = 31.599 \text{ mm}$$

APPENDIX D

Optimization for a 5-element low-pass equalizer (pi-section consisting of C_1, C_2, C_3, L_1, L_2).
The following calculation was written using Mathcad 5.0.



Width (W) of the Microstrip line given the impedance Z_0

Dielectric constant: $\epsilon_r := 2.33$

Thickness of the board (in inches) $d_{\text{inch}} := 0.125$

Thickness of the board (in mm) $d := d_{\text{inch}} \cdot 25.4 \quad d = 3.175$

Speed of light: $c := 3 \cdot 10^{10} \quad \text{cm/sec}$

W = line width(mm); d = thickness of dielectric (mm); $r = W/d$

Calculate "r" ($=W/d$) as a function of Z_0 given ϵ_r (Poazar p. 185) .

$$A(Z_0) := \frac{Z_0}{60} \cdot \sqrt{\frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \cdot \left(0.23 + \frac{0.11}{\epsilon_r}\right)}$$

$$B(Z_0) := \frac{377 \cdot \pi}{2 \cdot Z_0 \cdot \sqrt{\epsilon_r}}$$

Poazar gives the following two equations for r depending on whether $r > 2$ or $r < 2$.

$$r_1(Z_0) := \frac{8 \cdot e^{A(Z_0)}}{e^{2 \cdot A(Z_0)} - 2} \quad \text{for } r < 2.$$

$$r_2(Z_0) := \frac{2}{\pi} \left[B(Z_0) - 1 - \ln(2 \cdot B(Z_0) - 1) + \frac{\epsilon_r - 1}{2 \cdot \epsilon_r} \cdot \left(\ln(B(Z_0) - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right) \right] \quad \text{for } r > 2.$$

The following equation for $r = W/d$ selects either r_1 or r_2 , depending on whether $r_1 < 2$ or $r_1 > 2$

$$r(Z_0) := \text{if}(r_1(Z_0) \leq 2, r_1(Z_0), r_2(Z_0))$$

Calculate width of high impedance, low impedance, and 50 Ω line

High impedance: $Z_H := 200$ (inductors)

W/d ratio: $r(Z_H) = 0.09709$

Define W_H $W_H := r(Z_H) \cdot d$

Line width for Z_H $W_H = 0.30825$ mm

Low impedance: $Z_L := 20$ (capacitors)

W/d ratio: $r(Z_L) = 9.95253$

Define W_L $W_L := r(Z_L) \cdot d$

Line width for Z_L $W_L = 31.599$ mm

Characteristic line impedance: $Z_0 := 50$

W/d ratio: $r(Z_0) = 2.97028$

Define W_0 $W_0 := r(Z_0) \cdot d$

Line width for Z_0 $W_0 = 9.431$ mm

Effective dielectric constant and β for Z_H and Z_L .

Define $a(r)$ such that:

$a(r) = 1$ if $0 \leq r \leq 1$

$a(r) = 0$ otherwise

$a(r) := \text{if}(r \leq 1, 1, 0)$

Effective dielectric constant: $\epsilon_e(r) := \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \cdot \left[\frac{1}{\sqrt{1 + \frac{12}{r}}} + a(r) \cdot 0.041 \cdot (1 - r)^2 \right]$

High impedance: $\epsilon_H := \epsilon_e(r(Z_H))$

$\epsilon_H = 1.747$

Phase velocity: $u_{pH} := \frac{c}{\sqrt{\epsilon_H}}$ $u_{pH} = 2.27 \cdot 10^{10}$

Low impedance: $\epsilon_L := \epsilon_e(r(Z_L))$

$$\epsilon_L = 2.113$$

Phase velocity: $u_{pL} := \frac{c}{\sqrt{\epsilon_L}} \quad u_{pL} = 2.064 \cdot 10^{10}$

Read from disk the data file for the laser diode. Specify the frequency f_i as the 1st column.

$P := \text{READPRN}(\text{comb_sht})$

$f := P^{<1>}$

$w := 2 \cdot \pi \cdot f$

$n := \text{length}(w)$

$n = 11$

$i := 1..n$

Impedances: $Z_0 = Z_6 = \text{I/O sections}$; $Z_1 = Z_3 = Z_5 = \text{capacitors}$; $Z_2 = Z_4 = \text{inductor}$

$$Z_1 := Z_L \quad Z_2 := Z_H \quad Z_3 := Z_L \quad Z_4 := Z_H \quad Z_5 := Z_L \quad Z_6 := Z_0$$

Propagation constants in the High and Low impedance materials (β)

$$\beta_H := \frac{2 \cdot \pi}{u_{pH}} \cdot f \quad (\text{Inductors})$$

$$\beta_L := \frac{2 \cdot \pi}{u_{pL}} \cdot f \quad (\text{Capacitors})$$

ABCD elements for the capacitors (1,3 & 5), and the inductors (2, 4)

$$\begin{aligned}
 A_1(l_1) &:= \overrightarrow{\cos(\beta_L \cdot l_1)} & A_3(l_3) &:= \overrightarrow{\cos(\beta_L \cdot l_3)} & A_5(l_5) &:= \overrightarrow{\cos(\beta_L \cdot l_5)} \\
 B_1(l_1) &:= j \cdot Z_1 \cdot \overrightarrow{\sin(\beta_L \cdot l_1)} & B_3(l_3) &:= j \cdot Z_3 \cdot \overrightarrow{\sin(\beta_L \cdot l_3)} & B_5(l_5) &:= j \cdot Z_5 \cdot \overrightarrow{\sin(\beta_L \cdot l_5)} \\
 C_1(l_1) &:= \frac{j \cdot \overrightarrow{\sin(\beta_L \cdot l_1)}}{Z_1} & C_3(l_3) &:= \frac{j \cdot \overrightarrow{\sin(\beta_L \cdot l_3)}}{Z_3} & C_5(l_5) &:= \frac{j \cdot \overrightarrow{\sin(\beta_L \cdot l_5)}}{Z_5} \\
 D_1(l_1) &:= \overrightarrow{\cos(\beta_L \cdot l_1)} & D_3(l_3) &:= \overrightarrow{\cos(\beta_L \cdot l_3)} & D_5(l_5) &:= \overrightarrow{\cos(\beta_L \cdot l_5)}
 \end{aligned}$$

$$\begin{aligned}
 A_2(l_2) &:= \overrightarrow{\cos(\beta_H \cdot l_2)} & A_4(l_4) &:= \overrightarrow{\cos(\beta_H \cdot l_4)} \\
 B_2(l_2) &:= j \cdot Z_2 \cdot \overrightarrow{\sin(\beta_H \cdot l_2)} & B_4(l_4) &:= j \cdot Z_4 \cdot \overrightarrow{\sin(\beta_H \cdot l_4)} \\
 C_2(l_2) &:= \frac{j \cdot \overrightarrow{\sin(\beta_H \cdot l_2)}}{Z_2} & C_4(l_4) &:= \frac{j \cdot \overrightarrow{\sin(\beta_H \cdot l_4)}}{Z_4} \\
 D_2(l_2) &:= \overrightarrow{\cos(\beta_H \cdot l_2)} & D_4(l_4) &:= \overrightarrow{\cos(\beta_H \cdot l_4)}
 \end{aligned}$$

ABCD matrices for the capacitors (1,3 & 5), and the inductors (2, 4)

$$\begin{aligned}
 M_1(l_1, i) &:= \begin{pmatrix} A_1(l_1)_i & B_1(l_1)_i \\ C_1(l_1)_i & D_1(l_1)_i \end{pmatrix} & M_2(l_2, i) &:= \begin{pmatrix} A_2(l_2)_i & B_2(l_2)_i \\ C_2(l_2)_i & D_2(l_2)_i \end{pmatrix} & M_3(l_3, i) &:= \begin{pmatrix} A_3(l_3)_i & B_3(l_3)_i \\ C_3(l_3)_i & D_3(l_3)_i \end{pmatrix} \\
 M_4(l_4, i) &:= \begin{pmatrix} A_4(l_4)_i & B_4(l_4)_i \\ C_4(l_4)_i & D_4(l_4)_i \end{pmatrix} & M_5(l_5, i) &:= \begin{pmatrix} A_5(l_5)_i & B_5(l_5)_i \\ C_5(l_5)_i & D_5(l_5)_i \end{pmatrix}
 \end{aligned}$$

ABCD matrix for the system

$$\begin{aligned}
 M(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= M_1(1_1, i) \cdot M_2(1_2, i) \cdot M_3(1_3, i) \cdot M_4(1_4, i) \cdot M_5(1_5, i) \\
 A(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= M(1_1, 1_2, 1_3, 1_4, 1_5, i)_{1,1} & B(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= M(1_1, 1_2, 1_3, 1_4, 1_5, i)_{1,2} \\
 C(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= M(1_1, 1_2, 1_3, 1_4, 1_5, i)_{2,1} & D(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= M(1_1, 1_2, 1_3, 1_4, 1_5, i)_{2,2}
 \end{aligned}$$

Scattering matrix elements for the equalizer from the system ABCD matrix

$$\begin{aligned}
 K(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= A(1_1, 1_2, 1_3, 1_4, 1_5, i) + \frac{B(1_1, 1_2, 1_3, 1_4, 1_5, i)}{Z_0} \dots \\
 &\quad + C(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot Z_0 + D(1_1, 1_2, 1_3, 1_4, 1_5, i) \\
 S_{11}(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= \frac{A(1_1, 1_2, 1_3, 1_4, 1_5, i) + \frac{B(1_1, 1_2, 1_3, 1_4, 1_5, i)}{Z_0}}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)} \dots \\
 &\quad + \frac{-C(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot Z_0 - D(1_1, 1_2, 1_3, 1_4, 1_5, i)}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)} \\
 S_{12}(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= \frac{2}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)} \\
 S_{21}(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= \frac{2}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)} \\
 S_{22}(1_1, 1_2, 1_3, 1_4, 1_5, i) &:= \frac{-A(1_1, 1_2, 1_3, 1_4, 1_5, i) + \frac{B(1_1, 1_2, 1_3, 1_4, 1_5, i)}{Z_0}}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)} \dots \\
 &\quad + \frac{-C(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot Z_0 + D(1_1, 1_2, 1_3, 1_4, 1_5, i)}{K(1_1, 1_2, 1_3, 1_4, 1_5, i)}
 \end{aligned}$$

Read in the scattering matrix (reflection coef) for the laser diode at frequencies f_i

$$S_L := P^{<2>} + j \cdot P^{<3>}$$

$$m := \text{length}(S_L)$$

$$m = 11$$

Scattering matrix (reflection coef) for the generator at frequencies f_i

Impedance of the generator. $R_g := 50$

$$S_g := \frac{R_g - Z_0}{R_g + Z_0} \quad S_g = 0$$

Transducer power gain

$$S_2(1_1, 1_2, 1_3, 1_4, 1_5, i) := \left(S_{22}(1_1, 1_2, 1_3, 1_4, 1_5, i) + \frac{S_{21}(1_1, 1_2, 1_3, 1_4, 1_5, i)^2 \cdot S_g}{1 - S_{22}(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot S_g} \right)$$

$$T(1_1, 1_2, 1_3, 1_4, 1_5, i) := \frac{(|S_{21}(1_1, 1_2, 1_3, 1_4, 1_5, i)|)^2 \cdot [1 - (|S_g|)^2] \cdot [1 - (|S_{L_i}|)^2]}{(|1 - S_{11}(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot S_g|)^2 \cdot (|1 - S_2(1_1, 1_2, 1_3, 1_4, 1_5, i) \cdot S_{L_i}|)^2}$$

Calculate the component values (C_1 , etc.) that maximize the transducer power gain T at the frequencies f_i (in a least-squares sense).

Set the idealized value for T (this is arbitrary)

$$T_I := 0.30$$

Compute the sum of the squares, which is to be minimized

$$\text{SSE}(1_1, 1_2, 1_3, 1_4, 1_5) := \sum_{i=1}^n (T(1_1, 1_2, 1_3, 1_4, 1_5, i) - T_I)^2$$

Initial guess for parameters

$$l_1 = 0.675 \quad l_2 = 0.272 \quad l_3 = 0.619 \quad l_4 = 0.523 \quad l_5 = 1.583$$

Set up a solve block

Given

$$\text{SSE}(l_1, l_2, l_3, l_4, l_5) = 0$$

Dummy equations: (Mathcad needs 5 equations for 5 unknowns)

$$l_1 = 1 \quad l_2 = 2 \quad l_3 = 3 \quad l_4 = 4$$

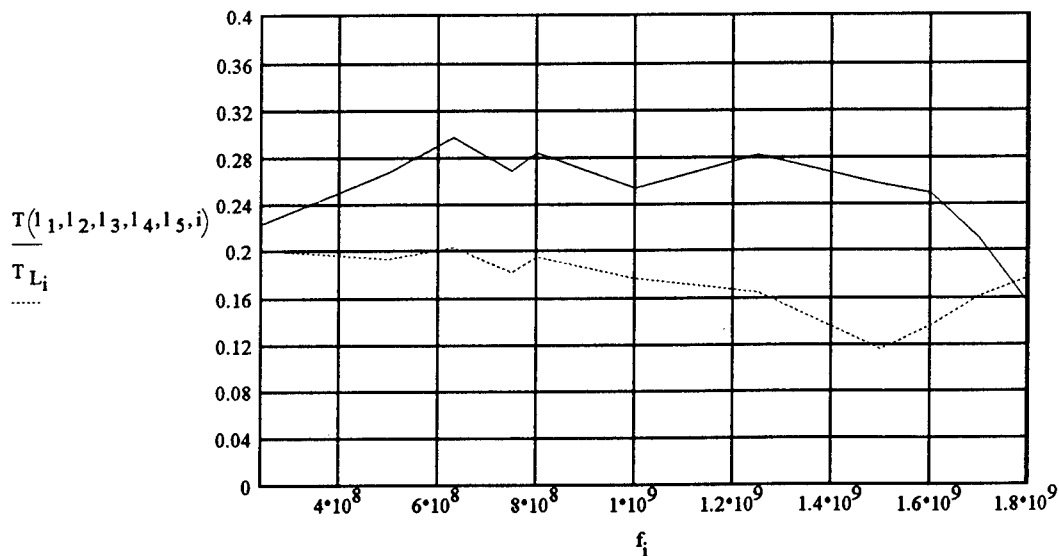
Minerr function gives best fit to data

$$\begin{bmatrix} l_1 \\ l_2 \\ l_3 \\ l_4 \\ l_5 \end{bmatrix} := \text{Minerr}(l_1, l_2, l_3, l_4, l_5) \quad \begin{bmatrix} l_1 \\ l_2 \\ l_3 \\ l_4 \\ l_5 \end{bmatrix} = \begin{bmatrix} 0.67491 \\ 0.27238 \\ 0.61918 \\ 0.52281 \\ 1.58304 \end{bmatrix}$$

Calculate the transducer power gain for the laser diode without the equalizer and the mean square error.

$$T_L := \left[1 - (|S_L|)^2 \right] \quad \frac{\text{SSE}(l_1, l_2, l_3, l_4, l_5)}{n - 2} = 0.00499$$

Plot the transducer power gain with and without the equalizer.



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